

(1)

1) mass oscillates on spring with given amplitude.

$$a) \omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{120 \text{ N/m}}{0.3 \text{ kg}}} = \boxed{20 \text{ s}^{-1} = \omega}$$

$$b) a_{\max} = \omega^2 A = (20 \text{ s}^{-1})^2 (0.04 \text{ m}) = \boxed{16 \text{ m/s}^2 = a_{\max}}$$

$$c) E = \frac{1}{2} k A^2 = \frac{1}{2} (120 \text{ N/m}) (0.04 \text{ m})^2 \\ = 9.6 \times 10^{-2} \text{ J} = \boxed{0.096 \text{ J} = E}$$

$$2) y(x, t) = (1.5 \text{ cm}) \sin \left[\left(2.5 \frac{\text{rad}}{\text{m}} \right) x + \left(20 \frac{\text{rad}}{\text{s}} \right) t \right]$$

a) travels toward -ve x ; as t increases x must decrease to hold phase const.

b) from standard form of wave:

$$y(x, t) = A \sin \left[\frac{2\pi}{\lambda} x \pm 2\pi f t \right]$$

we can write:

(2)

2) b) (cont.)

$$\lambda: \frac{2\pi}{\lambda} = 2.5 \frac{\text{rad}}{\text{m}} \Rightarrow \lambda = \frac{2\pi}{2.5 \text{ m}^{-1}} = \boxed{2.51 \text{ m} = \lambda}$$

$$f: 2\pi f = 20 \frac{\text{rad}}{\text{s}} \Rightarrow f = \frac{20 \text{ rad/s}}{2\pi} = \boxed{3.18 \text{ Hz} = f}$$

$$v: v = \lambda f = (2.51 \text{ m})(3.18 \text{ s}^{-1}) = \boxed{7.98 \text{ m/s} = v}$$

$$\begin{aligned} c) \quad y(0.8 \text{ m}, 0.1 \text{ s}) &= (0.015 \text{ m}) \sin \left[2.5 \frac{\text{rad}}{\text{m}} (0.8 \text{ m}) + 20 \frac{\text{rad}}{\text{s}} (0.1 \text{ s}) \right] \\ &= \boxed{-1.14 \times 10^{-2} \text{ m} = y(0.8, 0.1)} \end{aligned}$$

3)

$$I = 3.2 \times 10^{-6} \text{ W/m}^2$$

a) $\beta = ?$

$$\beta = (10 \text{ dB}) \log \left(\frac{3.2 \times 10^{-6} \text{ W/m}^2}{1 \times 10^{-12} \text{ W/m}^2} \right) = \boxed{65 \text{ dB} = \beta}$$

b) If 12 dB louder, what is factor on I ?

3) b) (CONT.)

$$\beta' = \beta + 12 = (10 \text{ dB}) \log \left(\frac{nI}{I_0} \right)$$

using $\log ab = \log a + \log b$

$$\beta + 12 = (10 \text{ dB}) \log n + \underbrace{(10 \text{ dB}) \log \left(\frac{I}{I_0} \right)}_{=\beta}$$

$$12 = (10 \text{ dB}) \log n$$

$$\frac{12}{10} = \log n$$

$$n = 10^{12/10} = \boxed{15.8 = n}$$

(4)

4) mosquito: $f_s = 600 \text{ Hz}$ $v_s = 3.5 \text{ m/s}$

$$f_o = f_s = \frac{1 \pm v_o/v}{1 \pm v_s/v}$$

a) Flying towards: $v_o = 0$, use - sign denom.

$$f_o = f_s \frac{1}{1 - v_s/v} = 600 \frac{1}{1 - \frac{3.5}{343}} = \boxed{606.2 \text{ Hz}}$$

b) Flying away: $v_o = 0$, use + sign in denom.

$$f_o = f_s \frac{1}{1 + v_s/v} = 600 \frac{1}{1 + \frac{3.5}{343}} = \boxed{593.9 \text{ Hz} = f_o}$$

5) $f_{\text{beat}} = |\Delta f| = |f_1 - f_2|$

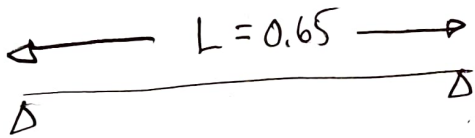
a) $f_{\text{beat}} = 6 \text{ Hz} = |512 - f_2|$

$$\Rightarrow f_2 = 506 \text{ Hz or } 518 \text{ Hz}$$

b) Δf increases with increase in f_2 ,
 f_2 must be higher!

$$f_2 = 518 \text{ Hz}$$

6)



$$\mu = 1.8 \times 10^{-3} \frac{\text{kg}}{\text{m}} \quad T = 95 \text{ N}$$

a) $v = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{95 \text{ N}}{1.8 \times 10^{-3} \frac{\text{kg}}{\text{m}}}} = 2.29 \times 10^2 \frac{\text{m}}{\text{s}} = v$

b) $f = n\left(\frac{v}{2L}\right) = \frac{2.29 \times 10^2 \frac{\text{m}}{\text{s}}}{2(0.65 \text{ m})} = 1.77 \times 10^2 \text{ Hz} = f$

6) (CONT.)

c) $f \propto v$, so we must double v , but
 $v \propto \sqrt{T}$ so to double v we must
increase T by a factor of 4!

$$T' = 4T = \boxed{380 \text{ N} = T'}$$

7) Fundamental $\Rightarrow n=1$, so either

a) open/open or closed/open

$$f = \frac{v}{2L}$$

$$= \frac{343 \text{ m/s}}{0.8} = 428 \text{ Hz}$$

↖ closer!

$$f = \frac{v}{4L}$$

$$= \frac{343 \text{ m/s}}{1.6} = 303 \text{ Hz}$$

$$\Rightarrow \boxed{\text{open/open}}$$

$$b) v = 2Lf$$

$$= 2(0.4 \text{ m})(430 \text{ Hz})$$

$$\boxed{v = 344 \text{ m/s}}$$

$$c) f_2 = 2 \frac{v}{2L} = 2 \frac{344 \text{ m/s}}{2(0.4 \text{ m})}$$

$$\boxed{f_2 = 860 \text{ Hz}}$$